Cambridge
IGCSE

## Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

## CANDIDATE

 NAMECENTRE NUMBER


CANDIDATE NUMBER
$\square$

Candidates answer on the Question Paper.
Additional Materials: Graphics Calculator

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
Do not use staples, paper clips, glue or correction fluid.
You may use an HB pencil for any diagrams or graphs.
DO NOT WRITE IN ANY BARCODES.
Answer all the questions.
You must show all relevant working to gain full marks for correct methods, including sketches.
In this paper you will also be assessed on your ability to provide full reasons and to communicate your mathematics clearly and precisely.
At the end of the examination, fasten all your work securely together.
The total number of marks for this paper is 24 .

Answer all the questions.

## INVESTIGATION

## SQUARES ON GRIDS

This investigation looks at the number of squares drawn on square grids

All squares are drawn using gridlines.

1 Here is a 2 by 2 grid.


Explain why there are 5 squares on a 2 by 2 grid.
$\qquad$
$\qquad$

2 Here is a 3 by 3 grid.


Complete these statements about the numbers of different sized squares on a 3 by 3 grid.

The number of 1 by 1 squares on a 3 by 3 grid is

The number of 2 by 2 squares on a 3 by 3 grid is
4
$\qquad$
$\qquad$
So the total number of squares on a 3 by 3 grid is $\qquad$
$\qquad$

3 Complete these statements about the numbers of different sized squares on a 4 by 4 grid. You may use the grids below to help you.

The number of 1 by 1 squares on a 4 by 4 grid is
The number of 2 by 2 squares on a 4 by 4 grid is
$\qquad$
$\qquad$

The number of 3 by 3 squares on a 4 by 4 grid is $\qquad$

The number of 4 by 4 squares on a 4 by 4 grid is $\qquad$

So the total number of squares on a 4 by 4 grid is 30


4 (a) Use your results from questions 1, $\mathbf{2}$ and $\mathbf{3}$ to help you complete this table.

|  | Number of.... |  |  |  |  |  | Total <br> Size of grid |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 by 1 <br> squares | 2 by 2 <br> squares | 3 by 3 <br> squares | 4 by 4 <br> squares | 5 by 5 <br> squares | 6 by 6 <br> squares | number of <br> squares |
| 1 by 1 | 1 |  |  |  |  |  | 1 |
| 2 by 2 |  |  |  |  |  |  | 5 |
| 3 by 3 |  | 4 |  |  |  |  |  |
| 4 by 4 |  |  |  |  |  |  | 30 |
| 5 by 5 |  |  |  |  |  |  |  |
| 6 by 6 |  |  |  |  |  |  |  |

(b) What is the mathematical name for the numbers in the $\mathbf{1}$ by $\mathbf{1}$ squares column?
(c) Work out the total number of squares on an 8 by 8 grid.
(d) Here is part of a table for an $n$ by $n$ grid.

It only has columns for 1 by 1 squares up to 6 by 6 squares.
Complete the table using expressions in terms of $n$.

|  | Number of.... |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Size of grid | 1 by 1 <br> squares | 2 by 2 <br> squares | 3 by 3 <br> squares | 4 by 4 <br> squares | 5 by 5 <br> squares | 6 by 6 <br> squares |
| $n$ by $n$ |  |  |  |  | $(n-4)^{2}$ |  |

(e) Write an expression, in terms of $n$, for the number of 12 by 12 squares on an $n$ by $n$ grid.
(f) (i) Find the number of 5 by 5 squares on a 20 by 20 grid.
(ii) The number of 5 by 5 squares on an $n$ by $n$ grid is 36 .

Find the value of $n$.

5 Here is a formula for the total number of squares, $T$, on an $n$ by $n$ grid.

$$
T=\frac{n^{3}}{3}+\frac{n^{2}}{2}+\frac{n}{6}+d
$$

(a) The total number of squares on a 1 by 1 grid is 1 .

Show that $d=0$.
(b) Show that the formula gives the correct total number of squares on a 4 by 4 grid.
(c) Find the total number of squares on a 10 by 10 grid.

6 (a) There are nine 7 by 7 squares on a 9 by 9 grid.
The diagrams show a 7 by 7 square drawn in two positions on a 9 by 9 grid.
In each diagram the same 2 by 2 square is shaded.


Consider the possible positions of the 7 by 7 square.
Explain how the shaded 2 by 2 square can be used to calculate the number of 7 by 7 squares on a 9 by 9 grid.
$\qquad$
$\qquad$
$\qquad$
(b) A square which is bigger than 9 by 9 is drawn on a square grid. It is only possible to draw 25 of these squares on the square grid.

Find two possible sizes for the square and the grid it is drawn on.
You may use the grid below to help you.

Square size $\qquad$ by y on a ......... by $\qquad$ grid.

Square size $\qquad$ by y $\qquad$ on a . by $\qquad$ grid.


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